

Labor Markets and Monetary Policy: A New Keynesian Model with Unemployment[†]

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We construct a utility-based model of fluctuations with nominal rigidities and unemployment. We first show that under a standard utility specification, productivity shocks have no effect on unemployment in the constrained efficient allocation. That property is also shown to hold, despite labor market frictions, in the decentralized equilibrium under flexible prices and wages. Inefficient unemployment fluctuations arise when we introduce real-wage rigidities. As a result, in the presence of staggered price setting by firms, the central bank faces a trade-off between inflation and unemployment stabilization, which depends on labor market characteristics. We draw the implications for optimal monetary policy. (JEL E12, E24, E52)

The New Keynesian model (the NK model, for short) has emerged as a powerful tool for monetary policy analysis in the presence of nominal rigidities. Its adoption as the backbone of the medium-scale models currently developed by many central banks and policy institutions is a clear reflection of its success. This popularity may be viewed as somewhat surprising given that standard versions of the NK paradigm do not generate movements in unemployment, only voluntary movements in hours of work or employment.¹

This provides the motivation for our paper. We extend the NK model by introducing a more realistic labor market, with frictions similar to those found in the Diamond-Mortensen-Pissarides search and matching model of unemployment (the DMP model, henceforth). This extension allows us to characterize the effects of productivity shocks on unemployment and inflation, and to show how these effects depend both on monetary policy and on the nature of labor market frictions. It also allows us to derive optimal monetary policy, and characterize its dependence on

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¹ Paradoxically, this was viewed as one of the main weaknesses of the RBC model, but was then exported to the NK model.

labor market frictions, to answer, for example, how monetary policy should differ, depending on whether the labor market is fluid (as in the United States) or sclerotic (as in continental Europe). As discussed in Section VI, a number of papers can be found in the literature that combine key elements of the NK and DMP frameworks.² In that context, we view the main contribution of our paper as the development of a highly tractable model combining four key ingredients: standard concave preferences, labor market frictions, real wage rigidities, and staggered price setting. The resulting model allows for a relatively simple and transparent analysis of monetary policy, and its associated trade-offs.

The paper is organized as follows. Section I sets up the basic model with frictions, leaving out nominal rigidities. We capture labor market frictions through hiring costs increasing in labor market tightness, defined as the ratio of hires to the unemployment pool. We then characterize the constrained-efficient allocation. Frictions lead to unemployment, but the unemployment rate is invariant to productivity shocks. The reason is that, as in the corresponding model without frictions, income and substitution effects cancel, leading to no change in employment, and in unemployment. Frictions do not affect this outcome.

Section II characterizes the decentralized equilibrium under alternative wage-setting mechanisms. As is well understood, frictions create a wage band, within which any real wage is consistent with private efficiency. Thus, we explore two alternatives. We first assume Nash bargaining. In this case, the unemployment rate is typically different from the constrained-efficient rate, but, like the latter, it is also invariant to productivity shocks. We then allow for more rigid real wages, and show that in this case, productivity shocks lead to inefficient fluctuations in unemployment. We characterize these fluctuations as a function of the labor market frictions and the degree of real wage rigidity.

Section III introduces nominal rigidities, in the form of staggering of price decisions by firms. We derive the relation between inflation and unemployment implied by the model, and contrast it to the standard NK formulation. Put crudely, the model implies a relationship between inflation and labor market tightness. This, in turn, implies a relationship between inflation and both the level and the change in the unemployment rate.

Section IV turns to the implications for monetary policy. It shows that, with flexible wages, unemployment can be stabilized by targeting inflation. With real wage rigidities, however, stabilizing unemployment in response to productivity shocks requires allowing for transitory movements in inflation. In that case, stabilizing inflation leads to large and inefficient movements in unemployment (recall that constrained-efficient unemployment is constant). It shows how the persistence of unemployment is higher in more sclerotic markets, i.e., markets in which the separation and the hiring rate are lower. It then derives optimal monetary policy, showing its dependence on labor market characteristics.

Section V offers two calibrations of the model, one aimed at capturing the United States, and the other aimed at capturing continental Europe, with its more sclerotic

² We should point out, however, that many of those papers have been written after a first draft of the present paper was completed and circulated (March 2006).

labor markets. In each case, it presents the implications of pursuing either inflation-stabilizing, unemployment-stabilizing, or optimal monetary policy. We also study the extent to which a simple interest rate rule can approximate the optimal policy outcomes.

Section VI indicates how our model relates to the existing, and rapidly growing, literature on the relative roles of labor market frictions, real wage rigidities, and nominal rigidities in shaping fluctuations. This literature started with Monika Merz's (1995) integration of labor market frictions in an RBC model, and now encompasses a number of medium-size DSGE models with labor market frictions, and real and nominal wage and price rigidities. We see the comparative strength of our paper as being in its simplicity. This simplicity allows for an analytical characterization of fluctuations, and an analytical derivation of optimal policy. It makes clear the separate roles of frictions, real wage rigidities, and monetary policy, in mediating the effects of productivity shocks on inflation and unemployment.

Section VII concludes.

I. The Basic Model

A. Assumptions

Preferences.—The representative household is made up of a continuum of members represented by the unit interval. The household maximizes

$$(1) \quad E_0 \sum \beta^t \left(\log C_t - \chi \frac{N_t^{1+\phi}}{1+\phi} \right),$$

where C_t is a CES function over a continuum of goods with elasticity of substitution ϵ , and N_t denotes the fraction of household members who are employed. The latter must satisfy the constraint

$$(2) \quad 0 \leq N_t \leq 1.$$

Note that such a specification of utility differs from the one generally used in the DMP model, where the marginal rate of substitution is assumed to be constant. Our specification is, instead, one often used in models of the business cycle, given its consistency with a balanced growth path and the direct parametrization of the inverse of the Frisch labor supply elasticity by ϕ .³

³ Our formulation is standard since at least Merz (1995). It assumes full risk sharing within a large family, and indivisible labor. The assumption of full risk sharing is, of course, a strong one, but it allows us to keep the analysis within the representative household paradigm, and avoid the complications that would result from introducing heterogeneity. Note also that the particular specification of labor disutility can be "microfounded" as the sum of members' utilities by assuming the disutility from working is χi^ϕ for member $i \in [0, 1]$. Then the sum of household members' disutilities is $\int_0^1 \chi i^\phi di = \chi (N_t^{1+\phi}/(1+\phi))$.

Technology.—We assume a continuum of monopolistically competitive firms indexed by $i \in [0, 1]$, each producing a differentiated final good. All firms have access to an identical technology

$$Y_t(i) = X_t(i),$$

where $X_t(i)$ is the quantity of the (single) intermediate good.

The latter is produced by a large number of identical, perfectly competitive firms, indexed by $j \in [0, 1]$, and with a production function⁴

$$X_t(j) = A_t N_t(j).$$

Variable A_t represents the state of technology, which is assumed to be common across firms and to vary exogenously over time.

Employment in firm j evolves according to

$$N_t(j) = (1 - \delta)N_{t-1}(j) + H_t(j),$$

where $\delta \in (0, 1)$ is an exogenous separation rate, and $H_t(j)$ represents the measure of workers hired by firm j in period t . Note that new hires start working in the period they are hired.

Labor Market: Flows and Timing.— At the beginning of period t there is a pool of jobless individuals available for hire, and whose size we denote by U_t . We refer to the latter variable as beginning-of-period unemployment (or just unemployment, for short). We make assumptions below that guarantee full participation, i.e., at all times all individuals are either employed or willing to work, given the prevailing labor market conditions. Accordingly, we have

$$(3) \quad U_t = 1 - N_{t-1} + \delta N_{t-1} = 1 - (1 - \delta)N_{t-1}.$$

Among those unemployed at the beginning of period t , a measure $H_t \equiv \int_0^1 H_t(j) dj$ are hired and start working in the same period. Aggregate hiring evolves according to

$$(4) \quad H_t = N_t - (1 - \delta)N_{t-1},$$

where $N_t \equiv \int_0^1 N_t(j) dj$ denotes aggregate employment.

We introduce an index of *labor market tightness*, x_t , which we define as the ratio of aggregate hires to unemployment

$$(5) \quad x_t \equiv \frac{H_t}{U_t}.$$

⁴ The motivation for the separation between final goods producers with monopoly power and perfectly competitive intermediate good producers is to avoid interactions between price setting and wage bargaining at the firm level.

This tightness index x_t will play a central role in what follows. It is assumed to lie within the interval $[0, 1]$. Only workers in the unemployment pool at the beginning of the period can be hired ($H_t \leq U_t$). In addition, and given positive hires in the steady state, shocks are assumed to be small enough to guarantee that desired hires remain positive at all times.

Note that, from the viewpoint of the unemployed, the index x_t has an alternative interpretation. It is the probability of being hired in period t , or, in other words, the *job finding rate*. Below we use the terms labor market tightness and job finding rate interchangeably.

Labor Market: Hiring Costs.— Hiring labor is costly. Hiring costs for an individual firm are given by $G_t H_t(j)$, expressed in terms of the CES bundle of goods. G_t represents the cost per hire, which is independent of $H_t(j)$ and taken as given by each individual firm.

While G_t is taken as given by each firm, it is an increasing function of labor market tightness. Formally, we assume

$$G_t = A_t B x_t^\alpha,$$

where $\alpha \geq 0$ and B is a positive constant.⁵ It is convenient, for later use, to define $g_t \equiv B x_t^\alpha$, so $G_t = A_t g_t$.

Note that, under our formalization, vacancies are assumed to be filled immediately by paying the hiring cost, which is a function of labor market tightness. By contrast, in standard formulations of the DMP model, the hiring cost is uncertain, with its expected value corresponding to the (per period) cost of posting a vacancy times the expected time to fill it. This expected time is an increasing function of the ratio of vacancies to unemployment, which can be expressed, in turn, as a function of labor market tightness. Thus, while the formalism used to capture the presence of hiring costs is different, both approaches share the basic characteristic that the cost of hiring is increasing in labor market tightness.⁶ Given that basic equivalence, and the fact that we are not interested in explaining vacancies, we have chosen our approach on the grounds of simplicity.

Finally, it is useful, for future reference, to define an alternative measure of unemployment, denoted by u_t , and given by the fraction of the population who are left without a job after hiring takes place in period t . Formally, and given our assumption of full participation, we have

$$u_t = U_t - H_t = 1 - N_t.$$

⁵ The motivation for the presence of A_t in the expression for G_t is to avoid effects of productivity shocks on the cost of hiring relative to the cost of producing, an effect we believe is best left out of the model. Alternatively, we could have assumed labor requirements per hire given by $g_t = B x_t^\alpha$, in which case, output for an individual firm would be given by $Y_t(j) = A_t(N_t(j) - g_t)$. All the qualitative results obtained below would go through in that case, though some expressions would be slightly different in the presence of real wage rigidities.

⁶ Note that under the matching function formulation, the expected cost of hiring an additional worker in the steady state is proportional to the average duration of a vacancy, which, in turn, is proportional to the ratio of vacancies to matches. Thus, and assuming a matching function of the form $H = Z U^\eta V^{1-\eta}$, we have that the expected hiring cost will be proportional to $V/H = Z^{1/(\eta-1)} (H/U)^{\eta/(1-\eta)}$, which takes the same form as our hiring cost function.

B. The Constrained-Efficient Allocation

We derive the constrained-efficient allocation by solving the problem of a benevolent social planner who faces the technological constraints and labor market frictions that are present in the decentralized economy. The social planner, however, internalizes the effect of variations in labor market tightness on hiring costs and, hence, on the resource constraint.

Given symmetry in preferences and technology, efficiency requires that identical quantities of each good be produced and consumed, i.e., $C_t(i) = C_t$ for all $i \in [0, 1]$. Furthermore, since labor market participation has no individual cost, but some social benefit (it lowers hiring costs for any given level of employment and hiring), the social planner will always choose an allocation with full participation (though not necessarily full employment, since higher employment generates disutility and raises hiring costs).

Hence, the social planner maximizes (1) subject to (2) and the aggregate resource constraint

$$(6) \quad C_t = A_t(N_t - Bx_t^\alpha H_t),$$

where H_t and x_t are defined in (4) and (5).

The optimality condition for the planner's problem can be written as

$$(7) \quad \chi C_t N_t^\phi \leq A_t - (1 + \alpha) A_t B x_t^\alpha + \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} A_{t+1} B x_{t+1}^\alpha (1 + \alpha(1 - x_{t+1})) \right\},$$

which holds with equality if $N_t < 1$. Henceforth, we restrict our analysis (both of the social planner's problem and the equilibrium) to allocations characterized by $N_t \in (0, 1)$ for all t (and, hence, positive unemployment).

Note that the left-hand side of (7) represents the marginal rate of substitution between labor and consumption, whereas the right-hand side captures the corresponding marginal rate of transformation. The latter has two components. The first component corresponds to the additional output, net of hiring costs, generated by a marginal employed worker. The second captures the savings in hiring costs resulting from the reduced hiring needs in period $t + 1$.⁷

The solution to this equation is easy to characterize. Consider, first, the case in which labor market frictions are absent (i.e., $B = 0$). In that case, we have $C_t = A_t N_t$, and the equilibrium condition (7) simplifies to

$$(8) \quad \chi N_t^{1+\phi} = 1$$

⁷ Note that hiring costs (normalized by productivity) at time t are given by $Bx_t^\alpha H_t$. The term Bx_t^α in (7) captures the increase in hiring costs resulting from an additional hire, keeping cost per hire unchanged. The term αBx_t^α reflects the effect on hiring costs of the change in the tightness index x_t induced by an additional hire (given H_t). The savings in hiring costs at $t + 1$ also have two components, both of which are proportional to $1 - \delta$, the decline in required hiring. The first component, Bx_{t+1}^α , captures saving resulting from a lower H_{t+1} , given cost per hire. The term $\alpha Bx_{t+1}^\alpha (1 - x_{t+1})$ adjusts the first component to take into account the lower cost per hire brought about by a smaller x_{t+1} (the effect of lower required hires, H_{t+1} , more than offsetting the smaller unemployment pool U_{t+1}).

if $\chi \geq 1$, or $N_t = 1$ if $\chi < 1$. In either case, the constrained-efficient allocation implies a level of employment invariant to productivity shocks. This invariance is the result of offsetting income and substitution effects on labor supply. Absent capital accumulation, consumption increases in proportion to productivity. Given our specification of preferences, this increase in consumption leads to an income effect that exactly offsets the substitution effect.

When labor market frictions are present (i.e., $B > 0$), the constrained-efficient allocation involves a *constant* job finding rate x^* , which, assuming positive unemployment in equilibrium, is implicitly given by the solution to

$$(9) \quad (1 - \delta B x^\alpha) \chi N(x)^{1+\phi} = 1 - (1 - \beta(1 - \delta))(1 + \alpha) B x^\alpha - \beta(1 - \delta) \alpha B x^{1+\alpha},$$

where $N(x) \equiv x/(\delta + (1 - \delta)x)$ is the level of employment given x . Thus, the constrained-efficient allocation implies a constant unemployment rate given by:⁸

$$u = \frac{\delta(1 - x^*)}{\delta(1 - x^*) + x^*}.$$

The implied levels of consumption and output are proportional to productivity, and given by $C_t^* = A_t N^*(1 - \delta B x^{*\alpha})$ and $Y_t^* = A_t N^*$.

Thus, the equilibrium inherits the main property of the equilibrium without frictions, namely the invariance of employment to productivity shocks. It does so because, at an unchanged employment level, both the marginal rate of substitution and the (social) marginal rate of transformation increase in the same proportion as productivity, given our assumptions on preferences and technology.

This invariance result is obviously a special one (e.g., it would no longer hold if we introduced capital accumulation). It is, however, very convenient for our purposes, since it establishes a simple benchmark. And it contains a more general lesson. Even in a model with labor market frictions, the behavior of the marginal rate of substitution remains central to the outcome.

The next step is to characterize the equilibrium in the decentralized economy. First, we consider the case of flexible prices, leaving the introduction of price rigidities to the following section.

II. Equilibrium under Flexible Prices

A. Price Setting

Let P_t be the price level (the price index associated with C_t), P_t^I be the price of the intermediate good, and W_t be the real wage (the wage in terms of the bundle of final consumption goods).

⁸ The condition for an interior solution to (9) is that the marginal rate of substitution be greater than the (social) marginal rate of transformation, both evaluated at full employment (i.e., evaluated at $N = 1$, $x = 1$, $H = \delta$):

$$\chi(1 - \delta B) > 1 - (1 + \alpha - \beta(1 - \delta))B.$$

Intermediate goods firms take the price of their good as given. Profit maximization requires that the following condition be satisfied for all t :

$$(10) \quad \left(\frac{P_t^I}{P_t} \right) A_t = W_t + G_t - \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} G_{t+1} \right\}.$$

Note that the left-hand side represents the real marginal revenue product of labor, while the right-hand side denotes the real marginal cost (including the component associated with hiring costs).

Profit maximization by final goods firms requires $P_t = \mathcal{M}P_t^I$ for all t , where $\mathcal{M} \equiv \epsilon/(\epsilon - 1)$ is the optimal gross markup. Using the previous result in (10) and reorganizing gives

$$(11) \quad Bx_t^\alpha = \left(\frac{1}{\mathcal{M}} - \frac{W_t}{A_t} \right) + \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} \frac{A_{t+1}}{A_t} Bx_{t+1}^\alpha \right\}.$$

Solving (11) forward, it follows that the rate at which labor is hired, and, hence, labor market tightness, depends on the expected discounted stream of marginal profits generated by an additional hire. Marginal profit depends, in turn, on the ratio of the wage to productivity.

Next, we turn to wage determination. The presence of labor market frictions generates a surplus associated with established employment relationships. The wage determines how that surplus is split between workers and firms. We consider two alternative wage-determination regimes.

B. Nash-Bargained Wages

The first regime, following much of the literature, is Nash bargaining. Note that the value of an employed member to a household, denoted by \mathcal{V}_t^N , is given by

$$\mathcal{V}_t^N = W_t - \chi C_t N_t^\phi + \beta E_t \left\{ \frac{C_t}{C_{t+1}} [(1 - \delta(1 - x_{t+1})) \mathcal{V}_{t+1}^N + \delta(1 - x_{t+1}) \mathcal{V}_{t+1}^U] \right\},$$

where \mathcal{V}_t^U is the value of an unemployed member, given in turn by

$$\mathcal{V}_t^U = \beta E_t \left\{ \frac{C_t}{C_{t+1}} [x_{t+1} \mathcal{V}_{t+1}^N + (1 - x_{t+1}) \mathcal{V}_{t+1}^U] \right\}.$$

It follows that the household's surplus from an established employment relationship, $\mathcal{S}_t^H \equiv \mathcal{V}_t^N - \mathcal{V}_t^U$, can be written as

$$(12) \quad \mathcal{S}_t^H = W_t - \chi C_t N_t^\phi + \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} (1 - x_{t+1}) \mathcal{S}_{t+1}^H \right\}.$$

On the other hand, the firm's surplus from an established employment relationship, denoted by \mathcal{S}_t^F , is simply given by

$$(13) \quad \mathcal{S}_t^F = A_t Bx_t^\alpha,$$

since any current worker can be immediately replaced with someone who is unemployed by paying the hiring cost, $G_t = A_t B x_t^\alpha$.

The Nash bargain must satisfy

$$S_t^H = \vartheta S_t^F,$$

where ϑ represents the *relative* bargaining power of workers. Combining this condition with (12) and (13) yields the following wage schedule

$$(14) \quad W_t = \chi C_t N_t^\phi + \vartheta \left(A_t B x_t^\alpha - \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} (1 - x_{t+1}) A_{t+1} B x_{t+1}^\alpha \right\} \right).$$

The bargained wage is equal to the marginal rate of substitution, plus, to the extent that workers have some bargaining power ($\vartheta > 0$) and labor market frictions are present ($B > 0$), an additional term reflecting labor market conditions. This term is increasing in current labor market tightness x_t (since this raises the firm's surplus associated with an existing relationship) and decreasing in expected future hiring costs, $A_{t+1} B x_{t+1}^\alpha$, and the probability of not finding a job if unemployed next period, $(1 - x_{t+1})$, since those raise the continuation value to an employed worker, thus reducing the required wage today.

Equation (11) implicitly gives the wage consistent with price setting. Equation (14) gives the wage consistent with Nash bargaining. Combining the two gives the equilibrium condition

$$(15) \quad \chi C_t N_t^\phi = \frac{A_t}{\mathcal{M}} - (1 + \vartheta) A_t B x_t^\alpha + \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} A_{t+1} B x_{t+1}^\alpha (1 + \vartheta(1 - x_{t+1})) \right\}.$$

It can easily be checked that the equilibrium, again, implies a constant job finding rate x , given implicitly by the solution to

$$(16) \quad (1 - \delta B x^\alpha) \chi N(x)^{1+\phi} = \frac{1}{\mathcal{M}} - (1 - \beta(1 - \delta))(1 + \vartheta) B x^\alpha - \beta(1 - \delta) \vartheta B x^{1+\alpha},$$

where, as before, $N(x) \equiv x/(\delta + (1 - \delta)x)$.⁹ This, in turn, implies a constant unemployment rate

$$u = \frac{\delta(1 - x)}{\delta(1 - x) + x}.$$

Consumption, output, and the real wage all vary in proportion to productivity. In particular, the real wage is given by

$$(17) \quad W_t = \left(\frac{1}{\mathcal{M}} - (1 - \beta(1 - \delta)) B x^\alpha \right) A_t.$$

⁹ The condition for an interior solution is now given by

$$\chi(1 - \delta B) > \frac{1}{\mathcal{M}} - (1 + \vartheta - \beta(1 - \delta)) B.$$

The condition for full participation is given by $W_t > \chi C_t$ for all t , since χC_t corresponds to the marginal rate of substitution evaluated at “full employment” (i.e., at $N_t = 1$). Under our assumption that wages are Nash-bargained, so employment is constant, this condition reduces to $((1/\mathcal{M}) - (1 - \beta(1 - \delta))g) > \chi N(x)(1 - \delta g)$. We shall assume that this condition holds throughout (and verify that it is the case for the calibrations below).

Note the two main characteristics of the equilibrium with Nash-bargained wages. The equilibrium unemployment rate generally differs from the constrained-efficient rate. Comparing (9) and (16) shows that the two unemployment rates coincide if

$$\mathcal{M} = 1 \quad \text{and} \quad \vartheta = \alpha,$$

i.e., in the absence of effective market power by final goods firms, and when the relative bargaining power of workers matches the elasticity of hiring costs relative to the labor market tightness index—a Hosios-like condition, familiar from DMP models.

Whether or not the equilibrium unemployment rate is equal to the constrained-efficient rate, it shares its property that it is invariant to productivity shocks. The source of the invariance, again, comes from the offsetting income and substitution effects, leading to a one-for-one response of the wage to productivity, and resulting in constant employment and unemployment rates.

This invariance result is different from the *Shimer puzzle*, the argument by Robert Shimer (2005) that the DMP model implies small movements in unemployment in response to movements in productivity. To see how the two results are related, return to the wage schedule under Nash bargaining, equation (14). Shimer’s result was derived under the assumption that the first term, the marginal rate of substitution, was constant. He then argued that, under reasonable values of the parameters characterizing labor market frictions, the second term—the term due to frictions—was likely to imply large movements in wages in response to productivity, and, by implication, small movements in profit, job creation, employment, and unemployment. In contrast, our neutrality result follows entirely from movements in the marginal rate of substitution. Under our assumptions, the marginal rate of substitution moves one-for-one with productivity, so employment does not change, and labor market frictions have no role to play. It is clear that, under more general assumptions (for example, in models where consumption increases less than one-for-one with productivity because of the presence of investment), both the marginal rate of substitution and labor market frictions will determine the wage response. Because the marginal rate of substitution is likely to increase with productivity (although not necessarily one-for-one as it does here), the wage response will be stronger than in the DMP model. Put another way, the Shimer puzzle will be even stronger than in the original Shimer set-up.

This large response of the wage to productivity movements appears counterfactual. This has led several authors to introduce some form of real wage rigidity in order to match the small movements in the wage and the large movements in

unemployment.¹⁰ Following their lead, Section IIC introduces wage rigidity, and analyzes its implications for equilibrium unemployment.

C. Real Wage Rigidities

As emphasized by Hall (2005), the presence of a surplus associated with existing relations implies that many wages may be consistent with equilibrium. More specifically, existing employment relationships will be privately efficient so long as they generate a positive surplus to both parties involved. Thus, and using the notation introduced in Section IIB, any wage path, such that $S_t^H \geq 0$ and $S_t^F \geq 0$ for all t , is consistent with equilibrium. Nash-bargaining generates only one such path.

In the context of our model, a sufficient condition for $S_t^H \geq 0$ is given by $W_t \geq \chi C_t N_t^\phi$ for all t , which is, in turn, already implied by the full participation condition $W_t \geq \chi C_t$. On the other hand, a sufficient condition for $S_t^F \geq 0$ is given by $W_t \leq (P_t^I/P_t)A_t = A_t/\mathcal{M}$ for all t , i.e., the existence of nonnegative profits (gross of hiring costs) for intermediate goods firms. It follows that any wage path satisfying

$$\chi C_t \leq W_t \leq \frac{A_t}{\mathcal{M}}$$

for all t is consistent with equilibrium. Note that, under our assumptions, the previous condition is satisfied when the wage is determined through Nash bargaining. In what follows, we shall assume the economy fluctuates in the neighborhood of the steady state under Nash bargaining. In that case, and to the extent that shocks are not too large, the previous condition will also be satisfied.

How to formalize real wage rigidity is still very much an open research question. To keep the analysis as simple as possible, we assume a wage schedule of the form

$$(18) \quad W_t = \Theta A_t^{1-\gamma},$$

where $\gamma \in [0, 1]$ is an index of real wage rigidities, and Θ is a positive constant.

Clearly, the above formulation is meaningful only if technology is stationary, an assumption we shall maintain here. Denoting the unconditional mean of A_t by A , we assume that $\Theta \equiv ((1/\mathcal{M}) - (1 - \beta(1 - \delta))Bx^\alpha)A^\gamma$. This implies that the mean wage coincides with the mean wage under Nash bargaining. Note that for $\gamma = 0$, the wage corresponds exactly to the equilibrium wage under Nash bargaining (as given by (17)). At the other extreme, when $\gamma = 1$, equation (18) corresponds to the canonical example of a rigid wage analyzed by Hall (2005).

Combining wage equation (18) with the equation for the wage implied by price setting, equation (11), gives us the equation for the *equilibrium under real wage rigidities*.

$$(19) \quad \Theta A_t^{-\gamma} = \frac{1}{\mathcal{M}} - Bx_t^\alpha + \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} \frac{A_{t+1}}{A_t} Bx_{t+1}^\alpha \right\}.$$

¹⁰ See Shimer (2005), Robert E. Hall (2005), and Mark Gertler and Antonella Trigari (2009). For a view that such rigidities may not be needed, see Marcus Hagedorn and Iourii Manovskii (2008).

Rearranging, and solving forward yields

$$(20) \quad Bx_t^\alpha = \sum_{k=0}^{\infty} (\beta(1-\delta))^k E_t \left\{ \Lambda_{t,t+k} \left(\frac{1}{M} - \Theta A_{t+k}^{-\gamma} \right) \right\},$$

where $\Lambda_{t,t+k} \equiv (C_t/C_{t+k})(A_{t+k}/A_t)$.

The previous equation makes clear the central role of labor market tightness x_t in this economy with labor market frictions and rigid real wages. As long as wages are not fully flexible ($\gamma > 0$), labor market tightness and, by implication, movements in employment and in unemployment, depend on current and anticipated productivity. Shimer (2005), Hall (2005), and the research that has followed their two articles, studied the implications of equations similar to (20) for fluctuations in wages, employment, and unemployment in response to productivity shocks. By contrast, our goal here is to study the implications in an economy with nominal rigidities, and the role for monetary policy. To do so, we need to introduce price stickiness. This is what we do in the next section.

III. Introducing Nominal Rigidities

Following much of the recent literature on monetary business cycle models, we introduce sticky prices in our model with labor market frictions using the formalism due to Guillermo A. Calvo (1983).¹¹ Each period, only a fraction $1 - \theta$ of the final goods producers, selected randomly, reset prices. The remaining final goods producers, with measure θ , keep their prices unchanged. Thus, the aggregate price level satisfies

$$(21) \quad P_t = ((1-\theta)(P_t^*)^{1-\epsilon} + \theta(P_{t-1})^{1-\epsilon})^{1/(1-\epsilon)},$$

where P_t^* denotes the price newly set by a final goods producer at time t .

The optimal price setting rule for a firm resetting prices in period t is given by

$$(22) \quad E_t \left\{ \sum_{k=0}^{\infty} \theta^k Q_{t,t+k} Y_{t+k|t} (P_t^* - \mathcal{M} P_{t+k} MC_{t+k}) \right\} = 0,$$

where $Y_{t+k|t}$ is the level of output in period $t+k$ for a firm resetting its price in period t , $\mathcal{M} \equiv \epsilon/(\epsilon-1)$ is the gross desired markup, MC_t is the real marginal cost for final goods producers, and $Q_{t,t+k} \equiv \beta^k (P_t/P_{t+k})(C_t/C_{t+k})$ is the relevant stochastic discount factor.

Real marginal cost is, in turn, given by P_t^I/P_t . Under the maintained assumption of flexible prices in the market for intermediate goods, using equation (10) for the

¹¹ As pointed out by one referee, the assumption of Calvo pricing in product markets leaves no room for bargaining between firms and consumers, in contrast with the assumed frictions in the labor market. See Hall (2008) for a recent attempt to overcome that asymmetry.

price of intermediate goods, and equation (18) for wage setting, real marginal cost is given by

$$(23) \quad MC_t = \Theta A_t^{-\gamma} + Bx_t^\alpha - \beta(1 - \delta) E_t \left\{ \frac{C_t}{C_{t+1}} \frac{A_{t+1}}{A_t} Bx_{t+1}^\alpha \right\}.$$

Equations (22) and (23) embody the essence of our framework:

- The optimal price setting equation (22) takes the same form as in the standard Calvo model, given the path of marginal costs. It leads firms to choose a price that is a weighted average of current and expected marginal costs, with the weights being a function of θ , the price stickiness parameter.
- The marginal cost in equation (23) depends on labor market frictions (as captured by hiring cost parameters B and α) and on real wage rigidities (measured by γ).¹²

Making progress requires log-linearizing the system, the task to which we now turn.

A. Log-linearized Equilibrium Dynamics

Let lower case variables with hats denote log deviations of the corresponding upper case variables from their steady state values.

- From equations (21) and (22), we get, after log-linearization around a zero inflation steady state, an expression for inflation,¹³

$$(24) \quad \pi_t = \beta E_t \{\pi_{t+1}\} + \lambda \widehat{mc}_t,$$

where $\lambda \equiv (1 - \beta\theta)(1 - \theta)/\theta$.

- From equation (23), we get an expression for marginal cost,

$$(25) \quad \widehat{mc}_t = \alpha g \mathcal{M} \hat{x}_t - \beta(1 - \delta) g \mathcal{M} E_t \{(\hat{c}_t - \hat{a}_t) - (\hat{c}_{t+1} - \hat{a}_{t+1}) + \alpha \hat{x}_{t+1}\} - \Phi \gamma \hat{a}_t,$$

where $\Phi \equiv \mathcal{M}W/A = 1 - (1 - \beta(1 - \delta))g\mathcal{M} < 1$.

¹² Under the assumption of sticky prices, the limiting case of $\gamma = 0$ in wage equation (18) no longer corresponds to the Nash-bargaining wage (which, among other things, will depend on how monetary policy is conducted). For our purposes, however, what matters is not so much full equivalence, but a common property. The lack of a tradeoff between inflation and unemployment stabilization in both cases.

¹³ See, e.g., Galí and Gertler (1999) for a derivation.

- From equation (5), we get an expression for labor market tightness as a function of current and lagged employment:

$$(26) \quad \delta \hat{x}_t = \hat{n}_t - (1 - \delta)(1 - x) \hat{n}_{t-1}.$$

- From equation (6), we get an expression for consumption:

$$(27) \quad \hat{c}_t = \hat{a}_t + \frac{1 - g}{1 - \delta g} \hat{n}_t + \frac{g(1 - \delta)}{1 - \delta g} \hat{n}_{t-1} - \frac{\alpha g}{1 - \delta g} \delta \hat{x}_t.$$

- From the first order conditions of the consumer (which we have ignored until now), we get

$$(28) \quad \hat{c}_t = E_t\{\hat{c}_{t+1}\} - (i_t - E_t\{\pi_{t+1}\} - \rho),$$

where $\rho \equiv -\log \beta$.

The equilibrium is characterized by equations (24)–(28), together with a process for productivity and a description of monetary policy.

B. Unemployment and Inflation

Before we turn to the analysis of alternative policies using the previous equilibrium conditions, we focus on the “Phillips curve” relation between unemployment and inflation implied by our model.

In order to facilitate intuition (and only in this subsection), we do so under two approximations. The first is that hiring costs are small relative to output (g is small), so we can approximate consumption by $\hat{c}_t = \hat{a}_t + \hat{n}_t$, and by implication, we can approximate $(\hat{c}_t - \hat{a}_t) - (\hat{c}_{t+1} - \hat{a}_{t+1})$ in equation (25) by $\hat{n}_t - \hat{n}_{t+1}$. The second is that the separation rate, δ , is small, so, from equation (26), fluctuations in \hat{x}_t are large relative to those in \hat{n}_t . This, in turn, implies that we can ignore the terms $\hat{n}_t - \hat{n}_{t+1}$ in equation (25). Using these two approximations, and the fact that, if δ is small, $\beta(1 - \delta) \approx \beta$, equation (25) can be approximated by:

$$(29) \quad \widehat{mc}_t = \alpha g \mathcal{M}(\hat{x}_t - \beta E_t\{\hat{x}_{t+1}\}) - \Phi \gamma \hat{a}_t.$$

Combining equation (29) and equation (24) then gives us *a relation between inflation, labor market tightness, and productivity*:

$$(30) \quad \pi_t = \alpha g \mathcal{M} \lambda \hat{x}_t - \lambda \Phi \gamma \sum_{k=0}^{\infty} \beta^k E_t\{\hat{a}_{t+k}\}.$$

Note that, despite the fact that expected inflation does not appear in (30), inflation is a forward-looking variable, through its dependence on current and future a_t 's, and current x_t , which itself depends on current and expected real marginal costs.¹⁴

¹⁴ This can be seen by solving (29) forward, to get $\alpha g \mathcal{M} \hat{x}_t = \sum_{k=0}^{\infty} \beta^k E_t\{\widehat{mc}_{t+k} + \Phi \gamma a_{t+k}\}$.

Using equation (26), letting $\hat{u}_t \equiv u_t - u$ denote the deviation (not the log deviation) of the unemployment rate (after hiring) from its steady state value, and using the approximation $\hat{u}_t = -(1-u)\hat{n}_t$, gives us a relation between labor market tightness and the unemployment rate:

$$(31) \quad (1-u)\delta\hat{x}_t = -\hat{u}_t + (1-x)(1-\delta)\hat{u}_{t-1}.$$

The relation of labor market tightness to current and lagged unemployment will play an important role in what follows. To see what it implies, consider two labor markets. One, with high values of both δ and x , so with high flows and low unemployment duration, which we shall call “fluid.” We think of that characterization as capturing the US labor market. The other, with low values of δ and x , so with low flows and high unemployment duration, which we shall call “sclerotic” and think of as capturing continental European labor markets. In the fluid labor market, $(1-x) \times (1-\delta)$ is small, so relative labor market tightness moves with the (negative) of the unemployment rate. In the sclerotic labor market, $(1-x)(1-\delta)$ is large, so relative labor market tightness moves more with the (negative) of the change in the unemployment rate. The intuition is as follows. In a fluid labor market, average flows are high and, given the constant separation rate, depend on the level of employment rate (equivalently, on the *level of unemployment*). Changes in employment (equivalently, changes in unemployment) lead to small relative changes in the flows, thus to small relative changes in labor market tightness. In a sclerotic labor market, average flows are low. Changes in employment (equivalently, in unemployment) lead to large relative changes in the flows. Thus, relative labor market tightness depends more on the change in employment (equivalently, on the *change in unemployment*).

Putting equations (30) and (31) together gives the relation between inflation and unemployment implied by our model. Assume, for simplicity, that productivity follows a stationary AR(1) process with autoregressive parameter $\rho_a \in [0, 1)$. We can then rewrite (30) as

$$(32) \quad \pi_t = \alpha g \mathcal{M} \lambda \hat{x}_t - \Psi \gamma \hat{a}_t,$$

where $\Psi \equiv \lambda \Phi / (1 - \beta \rho_a) > 0$. Thus, inflation depends positively on labor market tightness, and negatively (if $\gamma > 0$) on productivity. The higher the degree of real wage rigidity, or the more persistent the productivity process, the larger the effect of productivity on inflation.

Replacing market tightness by its expression from equation (31) gives

$$(33) \quad \pi_t = -\kappa \hat{u}_t + \kappa(1-\delta)(1-x)\hat{u}_{t-1} - \Psi \gamma \hat{a}_t,$$

where $\kappa \equiv \alpha g \mathcal{M} \lambda / \delta(1-u)$. Or equivalently,

$$\pi_t = -\kappa(1 - (1-\delta)(1-x))\hat{u}_t - \kappa(1-\delta)(1-x)\Delta\hat{u}_t - \Psi \gamma \hat{a}_t,$$

which highlights the negative dependence of inflation on both the level and the change in the unemployment rate, with the weights attached to each being a function

of the degree of fluidity of the labor market. The more sclerotic the labor market, the weaker the effect of the level of unemployment, and the stronger the effect of the change in unemployment.

Given that the constrained-efficient unemployment is constant, it would be best to stabilize both unemployment and inflation. Note, however, that, to the extent that the wage does not adjust fully to productivity changes ($\gamma > 0$), it is not possible for the monetary authority to fully stabilize both unemployment and inflation simultaneously. There is, to use the terminology introduced by Blanchard and Galí (2007), no *divine coincidence*. The reason is the same as in our earlier paper, the fact that productivity shocks affect the wedge between the natural rate—the unemployment rate that would prevail absent nominal rigidities—and the constrained-efficient unemployment rate. Stabilizing inflation, which is equivalent to stabilizing unemployment at its natural rate, does not deliver constant unemployment. Symmetrically, stabilizing unemployment does not deliver constant inflation.¹⁵

The next two sections examine the implications of alternative monetary policy regimes, both qualitative and quantitative. In doing so, we go back to the “exact” log-linearized model, characterized earlier.

IV. Unemployment, Inflation, and Monetary Policy

To characterize the effects of monetary policy, we must first derive the exact version of the Phillips curve. Note first that combining (26) and (27) we obtain

$$\hat{c}_t = \hat{a}_t + \xi_0 \hat{n}_t + \xi_1 \hat{n}_{t-1},$$

where $\xi_0 \equiv (1 - g(1 + \alpha))/(1 - \delta g)$, and $\xi_1 \equiv (g(1 - \delta))(1 + \alpha(1 - x))/(1 - \delta g)$. Replacing this expression, together with (26), into (25) gives an expression for marginal cost,

$$\widehat{mc}_t = h_0 \hat{n}_t + h_L \hat{n}_{t-1} + h_F E_t \{ \hat{n}_{t+1} \} - \Phi \gamma \hat{a}_t,$$

where

$$h_0 \equiv (\alpha g \mathcal{M} / \delta)(1 + \beta(1 - \delta)^2(1 - x)) + \beta(1 - \delta)g\mathcal{M}(\xi_1 - \xi_0)$$

$$h_L \equiv -(\alpha g \mathcal{M} / \delta)(1 - \delta)(1 - x) - \beta(1 - \delta)g\mathcal{M}\xi_1$$

$$h_F \equiv -\beta(1 - \delta)g\mathcal{M}((\alpha/\delta) - \xi_0).$$

¹⁵ In their seminal paper, Christopher J. Erceg, Dale W. Henderson, and Andrew T. Levin (2000), show that the coexistence of price and wage staggering generates a tradeoff between output gap and price inflation stabilization. Yet, as discussed in Michael Woodford (2003, ch. 6), one can define an appropriate weighted average of wage and price inflation for which the divine coincidence is restored. Furthermore, fully stabilizing that composite inflation measure (and, hence, the output gap) is nearly optimal for a wide range of plausible calibrations.

Replacing real marginal cost in equation (24) by the expression above, and using the fact that $\hat{u}_t = -(1 - u)\hat{n}_t$, gives the following Phillips curve relation between inflation to unemployment:

$$(34) \quad \pi_t = \beta E_t \{\pi_{t+1}\} - \kappa_0 \hat{u}_t + \kappa_L \hat{u}_{t-1} + \kappa_F E_t \{\hat{u}_{t+1}\} - \lambda \Phi \gamma \hat{a}_t,$$

where $\kappa_0 \equiv \lambda h_0 / (1 - u)$, $\kappa_L \equiv -\lambda h_L / (1 - u)$, and $\kappa_F \equiv -\lambda h_F / (1 - u)$.

A. Two Extreme Policies

We start by discussing two simple, but extreme, policies and their outcomes for inflation and unemployment.

Unemployment Stabilization.—Recall that in the constrained efficient allocation unemployment is constant. A policy that seeks to stabilize the gap between unemployment and its efficient level requires that $\hat{u}_t = 0$ for all t (and, hence, $\hat{n}_t = \hat{x}_t = 0$ for all t as well). Thus, it follows from (34) that

$$(35) \quad \pi_t = -\Psi \gamma \hat{a}_t,$$

where, as above, $\Psi \equiv \lambda \Phi / (1 - \beta \rho_a) > 0$. The stabilization of unemployment (and thus of hiring costs) makes the real marginal cost vary negatively with productivity, according to $\widehat{mc}_t = -\Psi \gamma a_t$, generating fluctuations in inflation. The amplitude of those fluctuations is increasing in the degree of wage rigidities γ (Ψ does not depend on γ), and in the persistence of the productivity process, ρ_a , but is decreasing in the degree of nominal rigidities (which is inversely related to λ).

Strict Inflation Targeting.—As (24) makes clear, setting $\pi_t = 0$ for all t requires that real marginal cost be fully stabilized, i.e., $\widehat{mc}_t = 0$ for all t . Given that variations in productivity are not fully offset by a proportional adjustment in the wage, stabilizing the real marginal cost requires that unemployment varies negatively with productivity, leading to a procyclical variation in the cost per hire that compensates the sluggish wage response. Imposing $\pi_t = 0$ for all t in (34) yields the following difference equation for unemployment:

$$\hat{u}_t = d_L \hat{u}_{t-1} + d_F E_t \{\hat{u}_{t+1}\} - d_a \hat{a}_t,$$

where $d_L \equiv \kappa_L / \kappa_0$, $d_F \equiv \kappa_F / \kappa_0$, and $d_a \equiv (\lambda \Phi \gamma / \kappa_0)$. The stationary solution takes the form

$$(36) \quad \hat{u}_t = b \hat{u}_{t-1} - c \gamma \hat{a}_t,$$

where $b \equiv (1 - \sqrt{1 - 4d_F d_L}) / (2d_F)$, and $c \equiv (\lambda \Phi / \kappa_0) / (1 - d_F(b + \rho_a))$.

Equation (36) points to a number of properties of strict inflation targeting policies. First, the volatility of unemployment under that policy regime is proportional to γ , the degree of wage rigidities, since the coefficients b and c are independent of

that parameter. Second, the unemployment rate displays some intrinsic persistence, i.e., some serial correlation beyond that inherited from productivity. The degree of intrinsic persistence is given by coefficient b , which was equal to $(1 - \delta)(1 - x)$ under the simplifying approximations made in the previous sections, and very close to it under plausible parameter calibrations, as shown below. Thus, the degree of intrinsic unemployment persistence depends critically on the separation rate δ and the steady state job finding rate x . In a “sclerotic” labor market, that is, a market with low x and low δ , and under strict inflation targeting, unemployment will display strong persistence, well beyond that inherited from productivity. Persistence will be much lower in a fluid labor market, a market with high x and high δ .¹⁶

Finally, note that the previous equation also characterizes the evolution of unemployment under flexible prices, since the allocation consistent with price stability replicates the one associated with the flexible price equilibrium.

B. Optimal Monetary Policy

We are now ready to characterize optimal policy. To simplify the analysis and avoid well understood but peripheral issues, we assume that unemployment fluctuates around a steady state value which corresponds to that of the constrained efficient allocation. This requires that the Hosios-like condition $\vartheta = \alpha$ is satisfied (together with our assumption on Θ introduced above), and that a constant employment subsidy is in place that exactly offsets the steady state price markup.¹⁷

As shown in Appendix A, a second order approximation to the welfare losses of the representative household around that steady state is proportional to

$$(37) \quad E_0 \sum_{t=0}^{\infty} \beta^t (\pi_t^2 + \alpha_u \hat{u}_t^2),$$

where $\alpha_u \equiv \lambda(1 + \phi)\chi(1 - u)^{\phi-1}/\epsilon > 0$.

Hence, the monetary authority will seek to minimize (37) subject to the sequence of equilibrium constraints given by (34), for $t = 0, 1, 2, \dots$. Clearly, given the form of the welfare loss function, the optimal policy will be somewhere between the two extreme policies discussed above. The first order conditions take the form:

$$(38) \quad 2\pi_t + \zeta_t - \zeta_{t-1} = 0$$

$$(39) \quad 2\alpha_u \hat{u}_t + \kappa_0 \zeta_t - \beta \kappa_L E_t \{\zeta_{t+1}\} - \beta^{-1} \kappa_F \zeta_{t-1} = 0$$

for $t = 0, 1, 2, \dots$, where ζ_t is the Lagrange multiplier associated with period t constraint, and where $\zeta_{-1} = 0$.

¹⁶ The hypothesis that more sclerotic markets might lead to more persistence to unemployment was explored empirically by Robert J. Barro (1988).

¹⁷ In the absence of such an assumption the equilibrium dynamics described below will hold only asymptotically, after a transition period in which the mean of inflation converges to zero only gradually. Alternatively, one can interpret it as the equilibrium outcome under an “optimal policy from the timeless perspective.” See Woodford (2003, ch. 7) for a detailed discussion.

The dynamical system describing the optimal policy is thus composed of (38) and (39), together with inflation equation (34), and a process for productivity a_t . The solution to that dynamical system can be obtained using standard methods for linear stochastic difference equations (see, e.g., Blanchard and Charles M. Kahn (1980)).

The next section gives a sense of the quantitative properties of the model, based on a rough calibration, and with a focus on the implications of different labor markets—fluid versus sclerotic—for monetary policy.

V. Calibration and Quantitative Analysis

We take each period to correspond to a quarter. For the parameters describing preferences, we assume values commonly found in the literature: $\beta = 0.99$, $\phi = 1$, and $\epsilon = 6$ (implying a gross steady state markup $\mathcal{M} = 1.2$).

We set $\lambda = 1/12$, which is consistent with an average duration of prices between three and four quarters, in accordance with much of the micro and macro evidence on price setting.¹⁸ Having no hard evidence on the degree of real wage rigidities, we set γ equal to 0.5, the midpoint of the admissible range.¹⁹

In order to calibrate α , we exploit a simple mapping between our model and the standard DMP model. In the latter, the expected cost per hire is proportional to the expected duration of a vacancy, which in the steady state is given by V/H , where V denotes the number of vacancies. Assuming a matching function of the form $H = ZU^\eta V^{1-\eta}$, we have $V/H = Z^{1/(\eta-1)}(H/U)^{\eta/(1-\eta)}$. Hence, the parameter α in our hiring cost function corresponds to $\eta/(1-\eta)$ in the DMP model. Since estimates of η are typically close to $1/2$, we assume $\alpha = 1$ in our baseline calibration.

We then choose the remaining coefficients to capture two different types of labor markets, through two different calibrations. Our baseline calibration attempts to capture the fluid US labor market. We choose parameters so the unemployment rate is equal to 5 percent, and the job finding rate x is equal to 0.7 (this quarterly job finding rate corresponds, approximately, to a monthly rate of 0.3, consistent with US evidence).²⁰ The alternative calibration attempts to capture the more sclerotic continental European labor market. We choose parameters so the unemployment rate is 10 percent, and $x = 0.25$ (consistent with a monthly job finding rate of 0.1).

¹⁸ Our calibration is consistent with the recent estimates of Emi Nakamura and Jón Steinsson (2008), which report a median price duration between 8 and 12 months. That median duration is considerably longer than the one uncovered earlier by Mark Bils and Peter J. Klenow (2004), due to the exclusion of sales in their analysis.

¹⁹ Under an overly strict interpretation of our model, γ can be obtained through a regression of real wage growth on productivity growth, which is exogenous in our model. Such a regression yields a coefficient between 0.3 and 0.4 using postwar US data, so a value for γ between 0.6 and 0.7. Stepping outside our model, obvious caveats apply, from the measurement of productivity growth, to the direction of causality. Perhaps most importantly, Christopher A. Pissarides (2009) and Christian Haefke, Marcus Sonntag, and Thijs van Rens (2007) argue that, in models with labor market frictions, job creation depends exclusively on the wage of new hires. They provide evidence suggesting that the latter is more sensitive to productivity changes than the average wage. In that case, the above estimate of the wage elasticity would overstate the relevant value for γ . That interpretation of that evidence, however, has been called into question by Gertler and Trigari (2009), on the grounds that it does not take into account compositional effects associated with variations over the cycle in the quality of jobs created.

²⁰ We compute the equivalent quarterly rate as $x_m + (1 - x_m)x_m + (1 - x_m)^2x_m$, where x_m is the monthly job finding rate. Note that this implicitly assumes that separations within the first quarter of an employment relationship are negligible.

These choices of x and u determine the separation rate, through the relation $\delta = ux/((1-u)(1-x))$. This yields a value for δ of 0.12 for the United States, and 0.04 for continental Europe.

The next step is to choose a value for B , which determines the *level* of hiring costs. Notice that, in the steady state, hiring costs represent a fraction $\delta g = \delta Bx^\alpha$ of gross domestic product (GDP). Lacking any direct evidence, we choose B so that under our baseline calibration for the United States, that fraction equals 1 percent of GDP, which seems a plausible upper bound. This implies $B = 0.01/(0.12)(0.7) \simeq 0.12$. We use this value of B for both calibrations.

Finally, we use equation (9), which gives the constrained-efficient value of x to tie down the value of χ . This implies $\chi \simeq 1.03$ for the United States, and $\chi \simeq 1.22$ for Europe.²¹ The implied value of α_u is 0.0237 for the US calibration and 0.0283 for Europe.²²

A. The Dynamic Effects of Productivity Shocks

Figures 1 and 2 summarize the effects of a productivity shock under alternative monetary policies, for each of the two calibrations of the labor market. In Figure 1, we assume a purely transitory shock ($\rho_a = 0$), which allows us to isolate the model's intrinsic persistence. Whereas, in Figure 2, we assume $\rho_a = 0.9$, a more realistic degree of persistence. In each figure, we display the responses of inflation and unemployment for both the US and European labor market calibrations. In all cases, we report responses to a 1 percent decline in productivity. All the responses are shown in percentage points, and in annual terms in the case of inflation.

We begin by discussing the case of a transitory shock.

The top left panel of Figure 1 shows the response of inflation to the adverse transitory productivity shock, under a policy that fully stabilizes unemployment. The response is nearly identical for both calibrations, implying a one-period rise in inflation of less than 20 basis points, with a subsequent return to its initial level once the shock dies out. The top right panel shows the response of unemployment to an identical adverse productivity shock, under a policy that fully stabilizes inflation. Unemployment rises by about 65 basis points on impact in the US calibration, and 50 basis points in the European one. Unemployment remains above its initial value well after the shock has vanished, with the persistence being significantly greater under the European calibration.

The bottom left and right panels of Figure 1 show, respectively, the response of inflation and unemployment under the optimal monetary policy. The optimal policy strikes a balance between the two extreme policies, and achieves a more muted response of both inflation and unemployment (note that, to facilitate comparison, the

²¹ Note that our model can only account for a higher efficient steady state unemployment rate in Europe by assuming a larger disutility of labor. Alternatively, we could have assumed an efficient steady state only for the United States, and impose the implied χ to the European calibration as well. In that case, however, the steady state unemployment for Europe would not be efficient and an additional linear term would appear in the loss function, complicating the analysis in an uninteresting (and well understood) way.

²² Such a (seemingly low) value is of the same order of magnitude as the weight on the output gap in calibrated loss functions found in the literature.

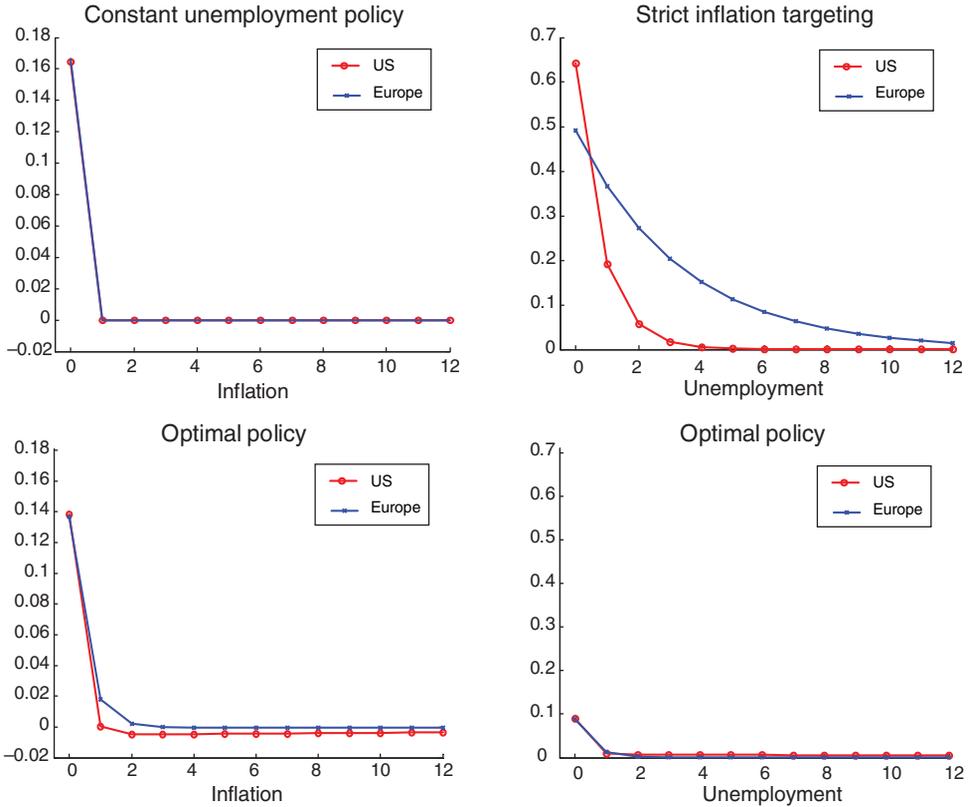


FIGURE 1. DYNAMIC RESPONSES TO A TRANSITORY PRODUCTIVITY SHOCK

scale of the graph is the same across policy regimes, for any given variable). The differences in the responses across the two calibrations are small. Interestingly, the persistence in both variables is tiny (though not zero) under both calibrations. Perhaps the most salient feature of the exercise is the substantial reduction in unemployment volatility under the optimal policy relative to a constant inflation policy, achieved at a relatively small cost in terms of inflation volatility.

Figure 2 displays corresponding results, but under the assumption that $\rho_a = 0.9$, a more realistic degree of persistence.

The response of inflation under the constant unemployment policy, shown in the top left panel of Figure 2, is now much larger, with an increase of about 150 basis points on impact under both calibrations. This amplification effect reflects the forward looking nature of inflation and the persistent anticipated effects on real marginal costs generated by the interaction of the shock and real wage rigidities. Note also that inflation inherits the persistence of the shock, as implied by (35).

The response of unemployment under a strict inflation targeting policy, shown on the top right panel, is also much larger with a persistent shock. The unemployment rate increases on impact by about 3 percentage points under both calibrations, a sizeable rise. In both cases, unemployment is highly persistent, and displays a prominent hump-shaped pattern, reaching a maximum rise of about 8 percentage points (!)

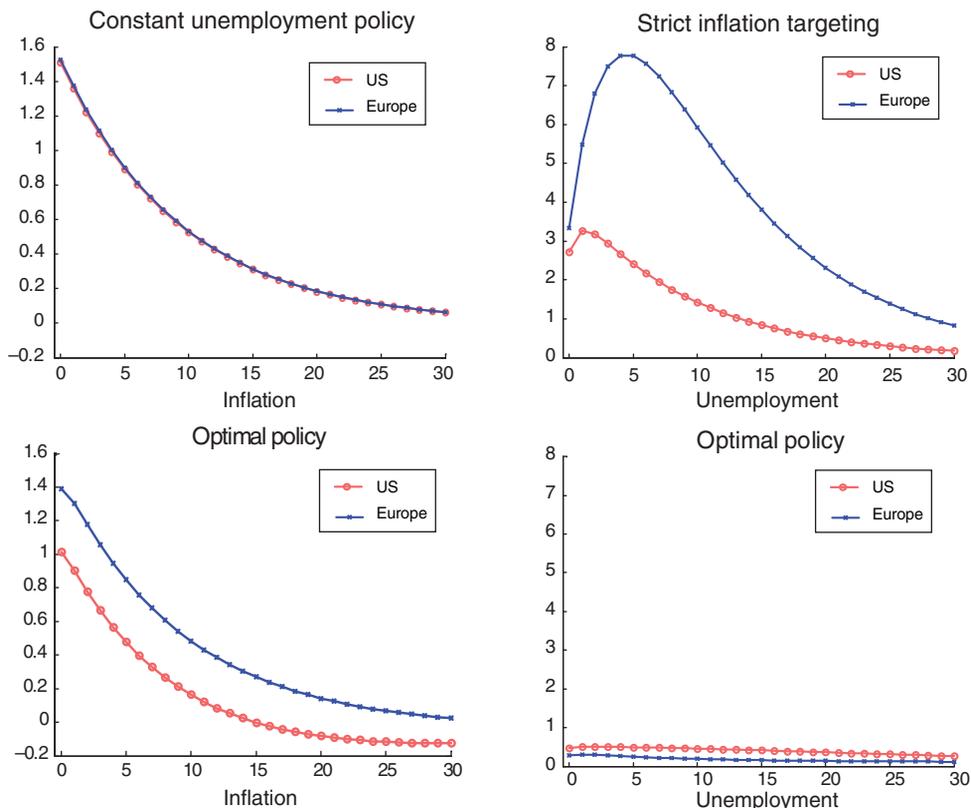


FIGURE 2. DYNAMIC RESPONSES TO A PERSISTENT PRODUCTIVITY SHOCK

in the case of Europe.²³ The degree of persistence is remarkably larger under the European calibration, for the reason discussed earlier: Persistence is higher if the labor market is more sclerotic.

The bottom panels show the behavior of inflation and unemployment under the optimal monetary policy. The increase in unemployment is 50 basis points under the US calibration, about half that size under the European one. Note that the size of such responses is several times smaller than under the strict inflation targeting policy. The price for having a smoother unemployment path is persistently higher inflation, with the latter variable increasing on impact by about 1 and 1.4 percentage points in the United States and Europe. We note that the optimal policy is “tougher on inflation” (i.e., more hawkish) in the United States relative to Europe. This is due to the larger cost, in the form of a persistent rise in unemployment, that results under the European calibration from policies that seek to stabilize inflation in response to an adverse productivity shocks, as illustrated by the extreme policy analyzed above.

Table 1 summarizes the main properties of the policies analyzed above under the two calibrations. More specifically, for each policy and calibration, the first

²³ While the size of this response may be viewed as unrealistically large, it is important to keep in mind that the policy assumed is also unrealistically extreme.

TABLE 1—PROPERTIES OF ALTERNATIVE POLICY RULES

	United States			Europe		
	$\sigma(\pi)$	$\sigma(u)$	<i>Loss</i>	$\sigma(\pi)$	$\sigma(u)$	<i>Loss</i>
Optimal	0.88	1.08	1.00	1.43	0.77	1.00
Constant u	1.48	0.00	1.87	1.52	0.00	1.08
Constant π	0.00	3.76	4.39	0.00	11.27	25.60
Optimized simple rule	1.07	1.11	1.34	1.47	0.42	1.04

two columns show the implied standard deviation of inflation and unemployment, with the standard deviation of productivity being normalized to unity (and given $\rho_a = 0.9$). In addition, we report the welfare loss implied by each policy relative to that implied by the optimal policy. One finding seems worth noting. The welfare losses associated with a strict inflation targeting policy appear to be very large relative to the optimal policy, especially so under the European calibration, which yields losses that are 25 times larger than under the optimal policy. This is again a consequence of the substantial volatility of unemployment required to keep inflation unchanged in the face of productivity shocks.

In addition to the two extreme policies and the optimal policy, Table 1 displays the statistics corresponding to an “optimized simple rule.” The latter is an interest rate rule of the form

$$i_t = \rho + \phi_\pi \pi_t + \phi_u \hat{u}_t,$$

where coefficients ϕ_π and ϕ_u are chosen, for each calibration, in order to minimize the welfare losses. The optimization is done numerically, searching over a grid spanning the intervals $\phi_\pi \in (1, 5]$ and $\phi_u \in [-5, 0]$.²⁴ The optimal coefficients are $\phi_\pi = 5$ and $\phi_u = -0.8$ for the US calibration, and $\phi_\pi = 2$, and $\phi_u = -0.6$ for the European calibration. The optimized simple rule puts a smaller weight on inflation stabilization under the European calibration, in a way consistent with our findings based on the optimal rule. In any event, as the results shown in the table make clear, following such a simple rule reduces considerably the losses relative to the extreme policies under both calibrations and, at least under the European one, comes close to replicating the welfare outcome obtained under the optimal policy.

VI. Relation to the Literature

Our model combines four main elements: (1) standard preferences (concave utility of consumption and leisure), (2) labor market frictions, (3) real wage rigidities, (4) price staggering. As a result, it is related to a large and rapidly growing literature.

²⁴ In the case of the US calibration, allowing for a larger range of values yields very large (in absolute values) coefficients for inflation and unemployment, with negligible gains in terms of welfare.

Merz (1995) and David Andolfatto (1996) were the first to integrate (1) and (2), by introducing labor market frictions in an otherwise standard RBC model. In particular, Merz derived the conditions under which Nash bargaining would or would not deliver the constrained-efficient allocation. Both models are richer than ours in allowing for capital accumulation, and in the case of Andolfatto, for having both an extensive margin (through hiring) and an intensive margin (through adjustment of hours) for labor. In both cases, the focus was on the dynamic effects of productivity shocks, and in both cases, the model was solved through simulations.

Arnaud Chéron and François Langot (2000), Carl E. Walsh (2003), and Trigari (2006), have integrated (1), (2), and (4), by allowing for Calvo nominal price setting by firms. Their models are, again, much richer than ours. Walsh allows for endogenous separations. Chéron and Langot, as well as Trigari, allow for both an extensive and an intensive margin for labor, with efficient Nash bargaining over hours and the wage. In addition Trigari considers “right to manage” bargaining, with the firm freely choosing hours *ex post*. Those models are too large to be analytically tractable, and are solved through simulations. The focus of Walsh and Trigari’s papers is on the dynamic effects of nominal shocks, while Chéron and Langot study the ability of the model with both productivity and monetary shocks to generate a Beveridge curve as well as a Phillips curve. More recent papers, by Walsh (2005), Trigari (2009), Stéphane Moyen and Jean-Guillaume Sahuc (2005), and Javier Andrés, Rafael Doménech, and Javier Ferri (2006) among others, introduce a number of extensions, from habit persistence in preferences, to capital accumulation, to the implications of Taylor rules. The models in these papers are relatively complex DSGE models, which need to be studied through calibration and simulations.

Shimer (2005) and Hall (2005) were the first to integrate (2) and (3). Shimer argued that, in the standard DMP model with Nash bargaining, wages were too flexible, and the response of unemployment to productivity shocks was too small. Hall (2005) showed, first, the scope for, and then the implications of, real wage rigidities in that class of models. These models differ from ours because of their assumption of linear preferences (in addition to their being purely real models). We have shown earlier the implications of this difference. But our results, using a standard utility specification, reinforce their conclusion that real wage rigidities are probably needed to explain fluctuations.

Gertler and Trigari (2009) have explored the implications of integrating (1), (2), and (3). Their model allows for standard preferences, labor market frictions, and real wage staggering à la Calvo. Being a real model, however, it has no room for nominal rigidities. Their model is, again, too complex to be solved analytically, and is studied through simulations. Their focus is on the dynamic effects of productivity shocks.

Two papers have explored a structure closely related to ours, but with staggered nominal wage setting rather than real wage rigidity. Carlos Thomas (2008) focuses on the role of monetary policy in that context, with implications substantially different from ours, which suggests that a more thorough exploration of the different implications of the two alternative assumptions is needed. Gertler, Luca Sala, and

Antonella Trigari (2008) estimate a model with standard preferences, labor market frictions, and both nominal wage and price rigidities.

The three papers closest to ours are by Michael V. Krause and Thomas A. Lubik (2007), Kai Christoffel and Tobias Linzert (2005), and Ester Faia (2008). They integrate (1) to (4), with standard preferences, labor market frictions, real wage rigidities, and nominal price staggering by firms. The three models are substantially richer than ours, and are solved through simulations. The main focus of Krause and Lubik is on the relation between inflation, marginal cost, and real wages, in the presence of matching frictions and endogenous separations. The main focus of Christoffel and Linzert is on inflation persistence in response to monetary policy shocks. The main focus of Faia is on the performance of simple monetary rules. Again, we see the comparative advantage of our paper as being in its simplicity, its analytical characterization of the effects of productivity shocks and optimal monetary policy in relation to labor market characteristics. We think that our analytical model is a needed step in the development and full understanding of these richer but more complex models.

VII. Conclusions

We have constructed a model with labor market frictions, real wage rigidities, and staggered price setting. We believe that the three ingredients above are all needed if one is to explain movements in unemployment, the effects of productivity shocks on the economy, and the role of monetary policy in shaping those effects.

From a positive point of view, we have shown that, in such an economy, a central variable is the degree of labor market tightness. A tighter labor market increases marginal cost, which, in turn, affects inflation. The relation between inflation and unemployment then depends on the relation between labor market tightness and unemployment, and this relation varies depending on labor market characteristics. In fluid labor markets such as the United States, labor market tightness varies more closely with unemployment. In sclerotic labor markets, such as those in continental Europe, labor market tightness varies more closely with the change in unemployment. These differences lead to important differences in the response of the economy to shocks. Under inflation stabilization, for example, the same productivity shock has more persistent effects in a sclerotic than in a fluid labor market.

From a normative point of view, we have shown that, in the presence of labor market frictions and real wage rigidities, strict inflation stabilization does not deliver the best monetary policy. As in Blanchard and Galí (2007), the reason is that distortions vary with shocks. As a result, strict inflation stabilization can lead to inefficient, large, and persistent, movements in unemployment in response to productivity shocks. These effects can be particularly large and persistent in sclerotic labor markets. Optimal monetary policy implies some accommodation of inflation, and limits the size of the fluctuations in unemployment.

APPENDIX A: DERIVATION OF THE WELFARE LOSS FUNCTION

Under our assumed utility specification we have

$$u(C_t) = \log C_t = c + \hat{c}_t$$

and

$$\begin{aligned} v(N_t) &= \chi \frac{N_t^{1+\phi}}{1+\phi} \\ &\simeq \chi \frac{N^{1+\phi}}{1+\phi} + \chi N^{1+\phi} \left(\frac{N_t - N}{N} \right) + \frac{1}{2} \phi \chi N^{1+\phi} \left(\frac{N_t - N}{N} \right)^2 \\ &\simeq \chi \frac{N^{1+\phi}}{1+\phi} + \chi N^{1+\phi} \hat{n}_t + \frac{1}{2} (1 + \phi) \chi N^{1+\phi} \hat{n}_t^2, \end{aligned}$$

where we have made use of the fact that up to second order $((N_t - N)/N) \simeq \hat{n}_t + \frac{1}{2} \hat{n}_t^2$. Hence, the deviation of period utility from its steady state value, denoted by U_t , is given by

$$(40) \quad U_t \simeq \hat{c}_t - \chi N^{1+\phi} \hat{n}_t - \frac{1}{2} (1 + \phi) \chi N^{1+\phi} \hat{n}_t^2.$$

Next, we derive an equation that relates, up to a second order approximation, \hat{c}_t and \hat{n}_t . Market clearing for good i requires that $A_t(N_t(i) - g(x_t)H_t(i)) = C_t(i)$. Integrating over i yields

$$\begin{aligned} A_t(N_t - g(x_t)H_t) &= \int_0^1 C_t(i) \, di \\ &= C_t \int_0^1 \frac{C_t(i)}{C_t} \, di \\ &= C_t \int_0^1 \left(\frac{P_t(i)}{P_t} \right)^{-\epsilon} \, di \\ &\equiv C_t D_t, \end{aligned}$$

where $D_t \equiv \int_0^1 ((P_t(i))/P_t)^{-\epsilon} \, di$.

Thus, we can write

$$\frac{C_t D_t}{A_t} = N_t - g(x_t) H_t.$$

Under the assumption that g is small enough, so that the terms involving $g\hat{n}_t$ are of second order, we have

$$\begin{aligned}
N_t - g(x_t)H_t &\simeq (1 - \delta g)N + N\left(\frac{N_t - N}{N}\right) - \alpha g N \delta \hat{x}_t - gN(\hat{n}_t - (1 - \delta)\hat{n}_{t-1}) \\
&\simeq (1 - \delta g)N + N\left(\hat{n}_t + \frac{1}{2}\hat{n}_t^2\right) - \alpha g N(\hat{n}_t - (1 - \delta)(1 - x)\hat{n}_{t-1}) \\
&\quad - gN(\hat{n}_t - (1 - \delta)\hat{n}_{t-1}) \\
&\simeq (1 - \delta g)N + \frac{1}{2}N\hat{n}_t^2 + N(1 - g(1 + \alpha))\hat{n}_t \\
&\quad + gN(1 - \delta)(1 + \alpha(1 - x))\hat{n}_{t-1},
\end{aligned}$$

where we have made use of equation (26) as well as the fact that $g'x = \alpha g$.

Thus,

$$\begin{aligned}
\frac{C_t D_t}{A_t(1 - \delta g)N} &= 1 + \frac{1}{2} \frac{1}{1 - \delta g} \hat{n}_t^2 + \frac{1 - g(1 + \alpha)}{1 - \delta g} \hat{n}_t \\
&\quad + \frac{g(1 - \delta)(1 + \alpha(1 - x))}{1 - \delta g} \hat{n}_{t-1}.
\end{aligned}$$

Taking logs, and approximating the resulting right-hand term up to second order using the fact that $\log(1 + \hat{z}_t) \simeq \hat{z}_t - \frac{1}{2}\hat{z}_t^2$, we have

$$(41) \quad \hat{c}_t = \hat{a}_t - d_t + \xi_0 \hat{n}_t + \xi_1 \hat{n}_{t-1},$$

where $\xi_0 \equiv (1 - g(1 + \alpha))/(1 - \delta g)$ and $\xi_1 \equiv (g(1 - \delta)(1 + \alpha(1 - x)))/(1 - \delta g)$.

LEMMA 1: *Up to a second order approximation, $d_t \equiv \log D_t \simeq (\epsilon/2) \text{var}_i(p_t(i))$.*

PROOF:

See Appendix B.

Using (40) and (41), we can write the expected discounted sum of period utilities as follows:

$$\begin{aligned}
E_0 \sum_{t=0}^{\infty} \beta^t U_t &\simeq -\frac{\epsilon}{2} E_0 \sum_{t=0}^{\infty} \beta^t \text{var}_i(p_t(i)) - \frac{1}{2} (1 + \phi) \chi N^{1+\phi} E_0 \sum_{t=0}^{\infty} \beta^t \hat{n}_t^2 \\
&\quad + E_0 \sum_{t=0}^{\infty} \beta^t (\xi_0 + \beta \xi_1 - \chi N^{1+\phi}) \hat{n}_t + t.i.p.,
\end{aligned}$$

where *t.i.p.* denotes terms independent of policy.

Assuming that the economy fluctuates around the efficient steady state, we can use (9) to show that the coefficient on \hat{n}_t equals zero.

The following result allows us to express the cross-sectional variance of prices as a function of inflation:

LEMMA 2: $\sum_{t=0}^{\infty} \beta^t \text{var}_i (p_t(i)) = (1/\lambda) \sum_{t=0}^{\infty} \beta^t \pi_t^2$.

PROOF:

Woodford (2003).

Combining the previous results, together with our definition of the unemployment rate u_t , we can write the welfare losses from fluctuations around the efficient steady state (ignoring terms independent of policy) as

$$\begin{aligned} \mathbb{L} &\equiv \frac{1}{2} E_0 \sum_{t=0}^{\infty} \beta^t \left[\frac{\epsilon}{\lambda} \pi_t^2 + (1 + \phi)\chi(1 - u)^{\phi-1} \hat{u}_t^2 \right] \\ &= \frac{1}{2} \frac{\epsilon}{\lambda} E_0 \sum_{t=0}^{\infty} \beta^t (\pi_t^2 + \alpha_u \hat{u}_t^2), \end{aligned}$$

where $\alpha_u \equiv \lambda(1 + \phi)\chi(1 - u)^{\phi-1}/\epsilon > 0$.

APPENDIX B: DERIVATION OF THE PRICE DISPERSION

From the definition of the price index, in a neighborhood of the zero inflation steady state:

$$\begin{aligned} 1 &= \int_0^1 \left(\frac{P_t(i)}{P_t} \right)^{1-\epsilon} di \\ &= \int_0^1 \exp\{(1 - \epsilon)(p_t(i) - p_t)\} di \\ &\simeq 1 + (1 - \epsilon) \int_0^1 (p_t(i) - p_t) di + \frac{(1 - \epsilon)^2}{2} \int_0^1 (p_t(i) - p_t)^2 di, \end{aligned}$$

thus implying

$$p_t \simeq \int_0^1 p_t(i) di + \frac{(1 - \epsilon)}{2} \int_0^1 (p_t(i) - p_t)^2 di.$$

By definition,

$$\begin{aligned}
 D_t &\equiv \int_0^1 \left(\frac{P_t(i)}{P_t} \right)^{-\epsilon} di \\
 &= \int_0^1 \exp \{ -\epsilon (p_t(i) - p_t) \} di \\
 &\simeq 1 - \epsilon \int_0^1 (p_t(i) - p_t) di + \frac{\epsilon^2}{2} \int_0^1 (p_t(i) - p_t)^2 di \\
 &\simeq 1 + \frac{\epsilon(1-\epsilon)}{2} \int_0^1 (p_t(i) - p_t)^2 di + \frac{\epsilon^2}{2} \int_0^1 (p_t(i) - p_t)^2 di \\
 &= 1 + \frac{\epsilon}{2} \int_0^1 (p_t(i) - p_t)^2 di.
 \end{aligned}$$

It follows that $d_t \simeq (\epsilon/2) \text{var}_i(p_t(i))$ up to a second order approximation.

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